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- [FAQ](#)
- [Search](#)
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- [Usergroups](#)
- [Profile](#)
- [You have no new messages](#)
- [Log out \[ denis\\_berthier \]](#)

## Abominable TRIAL-and-ERROR and lovely BRAIDS

Goto page [Previous](#) [1](#), [2](#), [3](#), [4](#), [5](#), [6](#), [7](#), [8](#), [9](#), [10](#) [Next](#)

[newtopic](#) [postreply](#) [Sudoku Players' Forums Forum Index -> Advanced solving techniques](#)

**Author**  
**denis\_berthier**

Posted: Wed Nov 25, 2009 6:02 am Post subject:



Joined: 19 Jun 2007  
Posts: 1123  
Location: Paris, France

Here is another braids example, this time with an unusually large number (6) of consecutive braids (usually, there are only a few braids lost amidst lots of whips)  
There is also an unusual number of chain patterns leading to several eliminations.  
Only braids are activated (we get the pB-NRCZT rating)  
I've manually edited the final cell of non-whip braids so that it looks better.

**Code:**

```

***** SudoRules version 13.7wbiB2 *****
....5.....567...28..23..6....78.....3...2...1.2.3.734.9...1...21...7....8...9. 306431
hidden-single-in-row r2 ==> r2c8 = 3
hidden-single-in-column c8 ==> r1c8 = 8
interaction column c8 with block b6 for number 5 ==> r5c9 <> 5, r5c7 <> 5, r4c9 <> 5
interaction column c8 with block b6 for number 4 ==> r5c9 <> 4, r5c7 <> 4, r4c9 <> 4
interaction column c4 with block b5 for number 5 ==> r6c6 <> 5, r5c6 <> 5
interaction row r5 with block b4 for number 5 ==> r6c1 <> 5, r4c3 <> 5, r4c1 <> 5
nrc-chain[2] n2{r1c2 r4c2} - n3{r4c2 r1c2} ==> r1c2 <> 9, r1c2 <> 1
nrc-chain[2] n2{r4c2 r1c2} - n3{r1c2 r4c2} ==> r4c2 <> 9, r4c2 <> 6
xyz-chain[3] {n6 n7}r7c5 - {n7 n4}r9c5 - {n4 n6}r8c5 ==> r9c6 <> 6, r8c6 <> 6, r7c6 <> 6
interaction block b8 with column c5 for number 6 ==> r5c5 <> 6, r4c5 <> 6
nrc-chain[3] n3{r8c6 r9c6} - n2{r9c6 r7c6} - n5{r7c6 r8c6} ==> r8c6 <> 4
nrc-chain[3] {n4 n6}r8c5 - {n6 n7}r7c5 - {n7 n4}r9c5 ==> r9c6 <> 4
interaction block b8 with column c5 for number 4 ==> r5c5 <> 4, r4c5 <> 4, r2c5 <> 4
nrczt-whip-cn[3] n9{r8c1 r8c2} - n9{r6c2 r6c6} - {n9r5c5 .} ==> r2c1 <> 9
nrczt-whip-bn[4] n3{r9c9 r8c9} - n8{r8c9 r8c2} - n9{r8c2 r8c1} - {n6r8c1 .} ==> r9c9 <> 6
nrczt-whip-rn[5] n6{r7c7 r7c5} - {n6 n4}r8c5 - n4{r9c5 r9c9} - n3{r9c9 r9c6} - {n2r9c6 .} ==> r9c7 <> 6
nrczt-braid-rc[7] n3{r9c9 r8c9} - {n3 n5}r8c6 - n5{r8c7 r3c7} - n7{r3c7 r1c7} - n5{r8c1 r5c1} - n7{r1c1 r9c1} - r9c3{n7 .} ==> r9c9 <> 9
nrczt-braid-rn[7] n5{r5c1 r5c3} - n7{r5c3 r5c2} - n4{r5c1 r5c6} - n9{r6c1 r6c6} - {n4 n1}r3c6 - {n1 n9}r3c2 - n9r8{c2 .} ==> r5c1 <> 9
nrczt-braid-cn[8] n8{r8c9 r7c9} - n8{r7c3 r5c3} - n5{r5c3 r5c1} - n4{r5c1 r5c6} - n4{r6c4 r1c4} - n3{r8c9 r9c9} - n4{r1c9 r3c9} - n5c9{r1c9 r3c9}
nrczt-braid-rc[8] n5{r5c1 r5c3} - {n5 n7}r9c3 - n7{r9c1 r1c1} - n7{r3c3 r3c7} - n5{r3c7 r3c9} - n8{r5c3 r7c3} - n6{r5c7 r4c9} - r7c9{n8}
nrczt-braid-rc[8] n8{r8c9 r7c9} - n8{r7c3 r5c3} - n5{r5c3 r5c1} - n7{r5c1 r5c2} - n5{r3c9 r3c7} - n7{r3c2 r3c3} - {n7 n5}r7c3 - r9c3{n7 .}
nrczt-whip-rc[9] n5{r3c9 r3c7} - n7{r3c7 r1c7} - n9{r1c7 r5c7} - n1{r5c7 r2c7} - {n1 n4}r2c1 - {n4 n7}r3c3 - n7{r7c3 r9c1} - n1{r9c1 r9c9}
nrczt-whip-rc[9] n1{r9c2 r3c2} - n7{r3c2 r5c2} - n7{r5c1 r1c1} - n2{r1c1 r1c2} - n3{r1c2 r1c3} - n9{r1c3 r3c3} - {n9 n4}r4c3 - n4{r5c3 r3c3}
hidden-single-in-block b7 ==> r9c2 = 1
nrczt-whip-rn[6] n5{r5c3 r5c1} - n7{r5c1 r5c2} - {n7 n9}r3c2 - n9{r3c3 r4c3} - n9{r6c2 r6c6} - {n8r6c6 .} ==> r5c3 <> 8
singles ==> r7c3 = 8, r8c9 = 8, r9c9 = 3, r8c6 = 3, r7c5 = 7
interaction row r7 with block b9 for number 6 ==> r8c7 <> 6
interaction column c9 with block b3 for number 4 ==> r3c7 <> 4, r2c7 <> 4, r1c7 <> 4
nrczt-whip-rn[2] n4{r5c1 r5c6} - {n4r2c6 .} ==> r4c1 <> 4, r6c1 <> 4
nrczt-chain[3] {n9 n6}r6c1 - n6{r9c1 r8c2} - n9{r8c2 r8c1} ==> r4c1 <> 9, r1c1 <> 9
nrczt-whip-rc[3] n6{r8c1 r8c2} - n9{r8c2 r8c1} - {n9r6c1 .} ==> r4c1 <> 6
singles ==> r4c1 = 2, r4c2 = 3, r1c2 = 2, r1c3 = 3
interaction block b1 with row r3 for number 9 ==> r3c7 <> 9, r3c6 <> 9
nrc-chain[3] {n1 n4}r3c6 - n4{r2c6 r2c1} - n1{r2c1 r1c1} ==> r1c6 <> 1
nrc-chain[3] n7{r1c7 r1c1} - n1{r1c1 r2c1} - {n1 n9}r2c7 ==> r1c7 <> 9
nrc-chain[2] n9{r5c7 r2c7} - n9{r1c9 r1c6} ==> r5c6 <> 9
nrc-chain[3] n9{r1c9 r1c6} - n6{r1c6 r1c4} - n6{r4c4 r4c9} ==> r4c9 <> 9
interaction block b6 with row r5 for number 9 ==> r5c5 <> 9, r5c3 <> 9, r5c2 <> 9
nrc-chain[3] n1{r4c9 r4c5} - n9{r4c5 r6c6} - n9{r1c6 r1c9} ==> r1c9 <> 1
nrc-chain[2] n7{r1c1 r1c7} - n1{r1c7 r1c1} ==> r1c1 <> 4
nrc-chain[3] n9{r6c6 r4c5} - {n9 n4}r4c3 - n4{r4c8 r6c8} ==> r6c6 <> 4
nrc-chain[2] n4{r6c4 r6c8} - n5{r6c8 r6c4} ==> r6c4 <> 6
nrc-chain[3] n9{r6c6 r4c5} - n1{r4c5 r4c9} - n6{r4c9 r4c4} ==> r6c6 <> 6
interaction row r6 with block b4 for number 6 ==> r5c2 <> 6
xy-chain[3] {n8 n1}r5c5 - {n1 n9}r4c5 - {n9 n8}r6c6 ==> r5c6 <> 8
xy-chain[3] {n1 n8}r5c5 - {n8 n9}r6c6 - {n9 n1}r4c5 ==> r5c6 <> 1
interaction column c6 with block b2 for number 1 ==> r2c5 <> 1
xy-chain[3] {n1 n9}r2c7 - {n9 n8}r2c5 - {n8 n1}r5c5 ==> r5c7 <> 1
interaction column c7 with block b3 for number 1 ==> r3c9 <> 1
nrc-chain[3] n6{r1c6 r5c6} - {n6 n9}r5c7 - n9{r5c9 r1c9} ==> r1c6 <> 9
singles
GRID 4918 SOLVED. LEVEL = pB-NRCZT9, MOST COMPLEX RULE = NRCZT9
123456789
456789132
879231564
234697851
785314926
961528347
348972615
592163478
617845293

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[Back to top](#)



**Pisaacson**

Posted: Fri Nov 27, 2009 1:11 pm Post subject:

Denis,

Joined: 02 Jul 2008  
Posts: 355  
Location: Campbell, CA

It looks like your example above did not include locked sets, so I used the "-Xprn" to exclude them from my braids run:

**Code:**

```
0000500000567000028002300600000078000003000200010203073409000100021000700008000090306431
```

12479	12379	3479	46	5	14689	1479	348	13489
149	5	6	7	1489	1489	149	348	2
8	179	479	2	3	149	14579	6	1459
-----								
24569	2369	3459	456	1469	7	8	45	14569
45679	6789	45789	3	14689	145689	14569	2	14569
4569	689	1	456	2	45689	3	45	7
-----								
3	4	578	9	67	256	256	1	568
569	689	2	1	46	3456	456	7	34568
1567	167	57	8	467	23456	2456	9	3456

```

1) r2c8 <= 3 hidden single in r2
2) r1c8 <= 8 hidden single in c8
3) r5c6 <> 5 pointing pair b8/c6
4) r6c6 <> 5 pointing pair b8/c6
5) r4c9 <> 4 claiming pair b6/c8
6) r5c7 <> 4 claiming pair b6/c8
7) r5c9 <> 4 claiming pair b6/c8
8) r4c9 <> 5 claiming pair b6/c8
9) r5c7 <> 5 claiming pair b6/c8
10) r5c9 <> 5 claiming pair b6/c8
11) r4c1 <> 5 claiming pair b4/r5
12) r4c3 <> 5 claiming pair b4/r5
13) r6c1 <> 5 claiming pair b4/r5
14) r1c2 <> 1 nrc[2x2]-braid n2{r1c2 r4c2} - {n3r4c2 .}
15) r1c2 <> 7 nrc[2x2]-braid n2{r1c2 r4c2} - {n3r4c2 .}
16) r1c2 <> 9 nrc[2x2]-braid n2{r1c2 r4c2} - {n3r4c2 .}
17) r4c2 <> 6 nrc[2x2]-braid n2{r4c2 r1c2} - {n3r1c2 .}
18) r4c2 <> 9 nrc[2x2]-braid n2{r4c2 r1c2} - {n3r1c2 .}
19) r4c5 <> 6 nrc[2x2]-braid {n6 n7}r7c5 - {n7 n4}r9c5
20) r5c5 <> 6 nrc[2x2]-braid {n6 n7}r7c5 - {n7 n4}r9c5
21) r7c6 <> 6 nrc[1x1]-braid n6{r7c5 r4c5}
22) r8c6 <> 6 nrc[1x1]-braid n6{r7c5 r4c5}
23) r9c6 <> 4 nrc[2x2]-braid n2{r9c6 r7c6} - n5{r7c6 r8c6}
24) r9c6 <> 6 nrc[1x1]-braid n6{r7c5 r4c5}
25) r2c1 <> 9 nrc[3x3]-braid n9{r8c1 r8c2} - n9{r6c2 r6c6} - n9{r4c5 r5c5}
26) r2c5 <> 4 nrc[3x3]-braid {n4 n6}r8c5 - {n6 n7}r7c5 - {n7r9c5 .}
27) r4c5 <> 4 nrc[3x3]-braid {n4 n6}r8c5 - {n6 n7}r7c5 - {n7r9c5 .}
28) r5c5 <> 4 nrc[3x3]-braid {n4 n6}r8c5 - {n6 n7}r7c5 - {n7r9c5 .}
29) r8c6 <> 4 nrc[1x1]-braid n4{r8c5 r4c5}
30) r9c9 <> 6 nrc[3x3]-braid n6{r7c7 r7c5} - n7{r7c5 r9c5} - n4{r9c5 r9c7}
31) r5c1 <> 9 nrc[4x5]-braid n5{r5c1 r5c3} - n4{r5c3 r5c6} - {n4 n1}r3c6 - {n1r3c2 .}
    [1]-strand { . n9r5c1} - n9{r6c1 r6c6}
32) r9c7 <> 6 nrc[3x5]-braid n6{r7c7 r7c5} - n7{r7c5 r9c5} - n4{r9c5 r9c7}
    [2]-strand { . n6r9c7} - n2{r9c7 r9c6} - n3{r9c6 r9c9}
33) r9c9 <> 5 nrc[4x5]-braid n5{r7c7 r3c7} - n7{r3c7 r1c7} - n7{r1c1 r5c1} - {n5r5c1 .}
    [1]-strand { . n5r9c9} - {n5 n7}r9c3
34) r5c1 <> 6 nrc[4x7]-braid n5{r5c1 r5c3} - n7{r5c3 r5c2} - n7{r3c2 r3c7} - n5{r3c7 r7c7}
    [3]-strand { . n6r5c1} - n5{r5c1 r5c3} - n8{r5c3 r7c3} - {n8 n5}r7c9
    [2]-strand { . n6r5c1} - n5{r5c1 r5c3} - {n5 n7}r9c3
35) r8c1 <> 6 nrc[5x7]-braid n9{r8c1 r8c2} - n8{r8c2 r8c9} - {n8 n6}r7c9 - n6{r4c9 r4c4} - {n6 n4}r1c4
    [2]-strand { . n6r8c1} - {n6 n4}r8c5 - {n4 n5}r8c7
36) r8c9 <> 6 nrc[4x7]-braid {n6 n4}r8c5 - n4{r8c7 r9c7} - n4{r1c7 r1c9} - {n4 n6}r1c4
    [2]-strand { . n6r8c9} - n8{r8c9 r7c9} - n5{r7c9 r3c9}
    [1]-strand { . n6r8c9} - n3{r8c9 r9c9}
37) r2c5 <> 1 nrc[4x5]-braid n1{r4c5 r5c6} - n4{r5c6 r5c3} - n5{r5c3 r5c1} - {n5 n9}r8c1
    [1]-strand { . n1r2c5} - {n1 n4}r2c1
38) r5c6 <> 1 nrc[1x1]-braid n1{r4c5 r5c5}
39) r5c1 <> 4 nrc[6x8]-braid n5{r5c1 r5c3} - n7{r5c3 r5c2} - {n7 n9}r3c2 - n9{r1c3 r4c3} - {n9 n1}r4c5 - {n1 n6}r4c9
    [2]-strand { . n4r5c1} - n5{r5c1 r5c3} - {n5 n7}r9c3
    [1]-strand { . n4r5c1} - {n4 n1}r2c1
40) r5c3 <> 4 nrc[6x8]-braid n5{r5c3 r5c1} - n7{r5c1 r5c2} - n8{r5c2 r6c2} - n9{r6c2 r4c3} - {n9 n1}r4c5 - {n1 n6}r4c9
    [2]-strand { . n4r5c3} - n5{r5c3 r5c1} - {n5 n9}r8c1
    [1]-strand { . n4r5c3} - n8{r5c3 r7c3}
41) r5c6 <= 4 hidden single in r5
42) r1c4 <= 4 hidden single in b2
43) r1c6 <= 6 hidden single in b2
44) r1c1 <> 9 nrc[4x8]-braid {n9 n5}r8c1 - {n5 n3}r8c6 - n3{r8c9 r9c9} - n4{r9c9 r8c9}
    [3]-strand { . n9r1c1} - {n9 n5}r8c1 - {n5 n7}r9c3 - {n7 n4}r3c3
    [2]-strand { . n9r1c1} - n9{r8c1 r8c2} - n8{r8c2 r8c9}
45) r2c6 <> 1 nrc[3x3]-braid {n1 n4}r2c1 - n4{r6c1 r4c3} - n3{r4c3 r1c3}
46) r3c6 <= 1 hidden single in b2
47) r9c2 <= 1 hidden single in c2
48) r2c7 <> 9 pointing pair b2/r2
49) r1c1 <> 7 nrc[4x6]-braid n1{r1c1 r2c1} - n4{r2c1 r6c1} - n6{r6c1 r6c2} - n8{r6c2 r6c6}
    [1]-strand { . n7r1c1} - n2{r1c1 r4c1}
    [1]-strand { . n7r1c1} - n7{r3c2 r5c2}
50) r1c3 <> 7 nrc[5x7]-braid n3{r1c3 r4c3} - n4{r4c3 r3c3} - {n4 n1}r2c1 - n1{r2c7 r1c9} - {n1r5c9 .}
    [3]-strand { . n7r1c3} - n3{r1c3 r4c3} - n9{r4c3 r5c3} - n9{r5c7 r1c7}
51) r1c7 <= 7 hidden single in r1
52) r3c2 <> 9 nrc[3x4]-braid n9{r8c2 r8c1} - n9{r6c1 r4c3} - {n4r4c3 .}
    [1]-strand { . n9r3c2} - n9{r3c7 r5c7}
53) r3c2 <= 7 naked single
54) r4c3 <> 9 pointing pair b1/c3
55) r5c3 <> 9 pointing pair b1/c3
56) r3c7 <> 4 nrc[6x8]-braid n4{r3c3 r4c3} - {n4 n5}r4c8 - {n5 n6}r4c4 - n6{r4c9 r5c9} - {n6 n8}r7c9 - n8{r8c9 r8c2}
    [1]-strand { . n4r3c7} - n5{r3c7 r3c9}
    [1]-strand { . n4r3c7} - n9{r3c7 r5c7}
57) r3c9 <> 9 nrc[2x3]-braid n9{r4c9 r5c7} - n1{r5c7 r4c9}
    [1]-strand { . n9r3c9} - {n9 n1}r1c9
58) r4c1 <> 6 nrc[4x7]-braid {n6 n5}r4c4 - {n5 n4}r4c8 - n4{r4c3 r3c3} - n4{r3c9 r8c9}
    [3]-strand { . n6r4c1} - n6{r5c2 r8c2} - n8{r8c2 r8c9} - n3{r8c9 r9c9}
59) r4c4 <> 5 nrc[5x6]-braid n6{r4c4 r4c9} - n1{r4c9 r4c5} - n9{r4c5 r4c1} - n9{r8c1 r8c2} - n8{r8c2 r8c9}
    [2]-strand { . n5r4c4} - n6{r4c4 r4c9} - n6{r5c7 r5c2}
60) r4c4 <= 6 naked single
61) r6c4 <= 5 naked single
62) r6c8 <= 4 naked single
63) r4c8 <= 5 hidden single in r4
64) r5c2 <> 6 pointing pair b6/r5
65) r1c9 <> 1 nrc[6x8]-braid {n1 n9}r4c9 - {n9 n6}r5c9 - {n6 n8}r7c9 - n8{r8c9 r8c2} - {n8 n9}r5c2 - {n9r5c5 .}
    [2]-strand { . n1r1c9} - n9{r1c9 r3c7} - n5{r3c7 r3c9}

```

singles from here on

123456789456789132879231564234697851785314926961528347348972615592163478617845293 puzzle 1 givens 26 nrczt 8.0

302.5493 m

I'm still working on the display and I know it's ugly, but it should be much easier to read than my prior versions. Some pointers:

- The initial braid on the step line " nnn) rccc <> d nrc[NxM]-braid" uses the number N to indicate the length of the primary strand that detected the conflict. The number M indicates the length of the supporting strands. If N=M, then it's really just a standard whip and there should be no supporting strands listed after it.
- Supporting strands follow the initial braid and they are presented in descending length. For reasons hard to explain, each begins with the z-target, which you can ignore. You have to read the original braid in order to "see" the common runs and unique truths.

The final score for my solution is 8. I ran the braids through a separate validation program and it concurs that they are all individually valid, so I'm slowly comparing each one ma

Cheers,  
Paul

[Back to top](#)

[profile](#) [pm](#)

**denis\_berthier**

Posted: Mon Nov 30, 2009 8:37 am Post subject:

**Allan,**

Joined: 19 Jun 2007  
Posts: 1123  
Location: Paris, France

For any puzzle P, one can define the minimal depth of T&E (in my sense, as defined at the start of this thread) necessary to solve it. **T&E-depth(P) is an intrinsic property of P**

I've shown that all the puzzles produced by random generators, in a total sample size of ~ 10 million, have depth 0 or 1.

Based on gsf's collection of hardest, I've also shown that only 5537 known puzzles have depth 2 and no known puzzle has depth > 2 (even the few with backdoor-size 3).  
Of course, this doesn't prove that there can't exist puzzles at depth 3, but if there are, they must be very rare.

Now, considering your approach, you have a notion of rank and, for each puzzle P, one can define **rank(P), an intrinsic property of P**: it is the smallest r such that P can be solved with rank ≤ r.

AFAIK, all the patterns you've been using have ranks 0, 1 or 2.

I'm therefore wondering (just a question, not yet a conjecture): do we have **T&E-depth(P) = rank(P)**?

How could this be tested? It depends on your answer to the following question: can you disable rank 2 (and above) patterns in your solver?

If so, there are several tests we could do:

- you could check whether you can solve all the puzzles in Sudogen0\_1M at ranks 0 or 1 - or even all the puzzles published on my web pages for all the kinds of generators. (Sorry, I checked this by solving all of them with nrczt-whips.)[Edit: on second thoughts, this is useless, as it should be easy to prove that any braid has rank 1.]
- we could try gsf's collection and compare the lists of puzzles solved at depths 0/1 and with ranks 0/1.

[Back to top](#)

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**Allan Barker**

Posted: Mon Nov 30, 2009 5:06 pm Post subject:

Joined: 21 Feb 2008  
Posts: 485  
Location: Bangkok

Hi Denis,

**Denis Berthier wrote:**

Now, considering your approach, you have a notion of rank and, for each puzzle P, one can define rank(P), an intrinsic property of P: it is the smallest r such that P can be solved with rank ≤ r.  
AFAIK, all the patterns you've been using have ranks 0, 1 or 2.

I'm therefore wondering (just a question, not yet a conjecture): do we have **T&E-depth(P) = rank(P)**?

I don't see a connection between rank, which is a static property of logic, and the number of assumed clues needed for a TE backtrack algorithm to solve a puzzle. For example, a backtracking(n=0) doesn't compute 😊.

But rank does represent a degree of freedom of sorts and rank 2 can eliminate some candidates that rank 1 can't, so there must be a relation between rank and solvability, as you

**Denis Berthier wrote:**

How could this be tested?

As far as a relation to T&E, **T&E-depth(0) <> rank(0)**, so no comparison. Rank and solvability is a different question.

**Denis Berthier wrote:**

can you disable rank 2 (and above) patterns in your solver?

Yes, but other properties may overshadow the effects of rank in any kind of large batch testing. Group links are a good example, as they can produce shorter paths with little logic. Different methods/rank on a puzzle by puzzle or even a candidate by candidate basis. This way you see what logical form makes a difference. I think I can find a couple of good ex

[Back to top](#)

[profile](#) [pm](#) [www](#)

**denis\_berthier**

Posted: Mon Nov 30, 2009 6:35 pm Post subject:

**Allan,**

Joined: 19 Jun 2007  
Posts: 1123  
Location: Paris, France

OK, the fish example is convincing and the equality can't hold.

Then take it in either of these ways:

- what's the smallest SER of puzzles that can't be solved with only patterns of rank 0 or 1?
- how many puzzles do you know that can't be solved with only patterns of rank 0 or 1?

[Back to top](#)

[profile](#) [pm](#) [www](#)

**Allan Barker**

Posted: Fri Dec 04, 2009 4:24 am Post subject:

**denis\_berthier wrote:**

**Allan,**  
OK, the fish example is convincing and the equality can't hold.

Then take it in either of these ways:

- what's the smallest SER of puzzles that can't be solved with only patterns of rank 0 or 1?
- how many puzzles do you know that can't be solved with only patterns of rank 0 or 1?

Sorry for the delay, I wanted to finish up some things first, see <http://www.sudoku.com/boards/viewtopic.php?p=84253#84253> for an answer.

[Back to top](#)

[profile](#) [pm](#) [www](#)

**denis\_berthier**

Posted: Fri Dec 04, 2009 7:17 am Post subject:

I can't see there any answer to my question.

Joined: 19 Jun 2007  
 Posts: 1123  
 Location: Paris, France

The kind of answer I was expecting is something like the table here:  
<http://www.sudoku.com/boards/viewtopic.php?t=6390&postdays=0&postorder=asc&start=44>.  
 It shows that almost all (and probably all) known puzzles can be solved at rank 0 or 1.

[Back to top](#)

[profile](#) [pm](#) [www](#)

**Allan Barker**

Posted: Sat Dec 12, 2009 2:43 pm Post subject:

**denis\_berthier wrote:**

Remember that gs's collection is ordered according to decreasing Q1 rating.  
 In the following table, the first column defines the sets of puzzles I consider: [.....]

**Code:**

```
Nb of puzzles solved:
FP family.....ECP+NS+HS.....ECP+NS+HS+BI.....SubsetRules+BI
Braids used.....nrczt-braids.....hinged-zt-braids.....hinged-zt-LS-braids
1-500.....0.....187.....443
501-1000.....0.....178.....460
1001-2000.....0.....331.....976
2001-3000.....0.....251.....953
3001-4000.....1.....233.....945
4001-5000.....1.....333.....930
5001-5500.....47.....348.....500
5501-6000.....434.....490.....500
6001-7000.....981.....1000.....1000
7001-8152.....1152.....1152.....1152
Total.....2616.....4505.....7859
Rest.....5536.....3647.....393
```

When the theory T in T&E(T) becomes more complex than ECP+NS+HS+BI, computation times are very long: Triplets and Quads are relatively rare patterns and, in our procedure must explore almost all the candidate hypotheses, sometimes several times (phase iteration). After puzzles solved by hinged-zt-braids are discarded, there is a collection; for each of them, T&E must try between 500 and 1,500 auxiliary puzzles; this makes ~ 3 to 4 million puzzles to deal with using the rules in T.

**Denis,**

As this seems to be the current subject, I have been trying to better understand some of the details. Most is clear but at the point referenced above, it's not clear to me which of the puzzles.

Were they solved,

1. using a not T&E solver that implements the full FP family or
2. using the T&E(FP) procedure discussed above, and applying the T&E theorem, or
3. using 1 or 2 depending on computational necessity?

This is purely computational question, I understand the T&E theorem and how it's applied, and also know this is not the final data.

Allan

[Back to top](#)

[profile](#) [pm](#) [www](#)

**denis\_berthier**

Posted: Sat Dec 12, 2009 3:13 pm Post subject:

**Allan Barker wrote:**

As this seems to be the current subject, I have been trying to better understand some of the details. Most is clear but at the point referenced above, it's not clear to me what was use to solve the puzzles.  
 Were they solved,  
 1. using a not T&E solver that implements the full FP family or  
 2. using the T&E(FP) procedure discussed above, and applying the T&E theorem, or  
 3. using 1 or 2 depending on computational necessity?  
 This is purely computational question, I understand the T&E theorem and how it's applied, and also know this is not the final data.

As has been clearly stated, all these data were obtained using the T&E(FP) vs braids(FP) equivalence theorem and computed with the T&E(FP) procedure.  
 As I have also clearly stated, neither the zt-braids(FP) nor the zt-whips(FP) have been implemented in SudoRules, except of course for the basic FP={NS HS}. They have been part of the puzzle.

So, if you imply that what you're trying to do in the "ribbon" thread is an implementation of zt-whips(FP), which are precisely defined patterns but have never been fully implemented.

Last edited by denis\_berthier on Sat Dec 12, 2009 5:10 pm; edited 1 time in total

[Back to top](#)

[profile](#) [pm](#) [www](#)

**denis\_berthier**

Posted: Sat Dec 12, 2009 4:54 pm Post subject:

[deleted: edit error]

Last edited by denis\_berthier on Sat Dec 12, 2009 5:11 pm; edited 1 time in total

[Back to top](#)

[profile](#) [pm](#) [www](#)

**Allan Barker**

Posted: Sat Dec 12, 2009 5:08 pm Post subject:

**denis\_berthier wrote:**

**Allan Barker wrote:**

As this seems to be the current subject, I have been trying to better understand some of the details. Most is clear but at the point referenced above, it's not clear to me what the two approaches was use to solve the puzzles.  
 Were they solved,  
 1. using a not T&E solver that implements the full FP family or  
 2. using the T&E(FP) procedure discussed above, and applying the T&E theorem, or  
 3. using 1 or 2 depending on computational necessity?

This is purely computational question, I understand the T&E theorem and how it's applied, and also know this is not the final data.

As has been clearly stated, all these data were obtained using the T&E(FP) vs braids(FP) equivalence theorem and computed with the T&E(FP) procedure. As I have also clearly stated, neither the zt-braids(FP) nor the zt-whips(FP) have been implemented in SudoRules. They have been partly implemented in Paul's solver

OK, that's clear. If you read the written portion of what I quoted, the wording leads me to think it was a mixture, possibly with Paul's help.

**denis\_berthier wrote:**

So, if you imply that what you're trying to do in the "ribbon" thread is an implementation of zt-whips(FP), which are precisely defined patterns but have never been fully agree.

I have no need to make implications and prefer to speak directly. The reason I am trying to learn more is to see how we would be able to make any comparisons, if we want to.

Cheers.

[Back to top](#)

[profile](#) [pm](#) [www](#)

**denis\_berthier**

Posted: Sat Dec 12, 2009 5:26 pm Post subject:

Paul wasn't informed of my work on whips(FP) and braids(FP) (definitions, theorems, stats) before I published it.

**Allan Barker wrote:**

The reason I am trying to learn more is to see how we would be able to make any comparisons, if we want to.

I have given the basis for such comparisons in your "ribbon" thread.

It is obvious and it is based on the lexicon already mentioned there (which you haven't denied):

**look-back => using the (z)t extension**

**Truth => the content of a 2D-cell (i.e. rc-, rn-, cn- or bn- cell)**

**overlapping truths => different 2D-cells sharing (at least) a candidate (cells which must therefore be in different 2D spaces)**

**logic => pattern**

**logic integration => accepting patterns as right-linking objects instead of mere right-linking candidates - as in zt-whips(FP).**

They show clearly that, when your renaming of everything is cancelled and except perhaps a few cases of doubly linked AAAAL/HS, your "ribbons", whose fundamental property is not different from zt-whips(FP) or zt-braids(FP) if you allow branching.

[Back to top](#)

[profile](#) [pm](#) [www](#)

**Mauricio**

Posted: Fri Jan 08, 2010 7:19 pm Post subject:

Here is a procedure that calculates a lower bound of the pBrating of a puzzle.

I will use some of Denis notations (nrc linked, 2D cell).

For a candidate  $R0^{i1}$ , an **MBraid** (M for Mauricio) of length  $n$  for  $R0^{i1}$  is the following sequence of sets of candidates  $\{R0^{i1}\}, \{R1^{i1}, R1^{i2}, \dots, R1^{im1}\}, \{R2^{i1}, \dots, R2^{im2}\}, \dots, \{Rn^{i1}, \dots, Rn^{imn}\}$  properties:

1. For every  $i > 0$ ,  $\{Ri^{i1}, Ri^{i2}, \dots, Ri^{imi}\}$  are **all** the possible candidates such that for every  $Ri^{ij}$ , there exists a 2D cell that contains it and that every other candidate in this cell  $k < i$  ( $k=0$  is possible).
2.  $Ri^{ij}$  is different from a candidate  $Rk^{kl}$  if  $i < k$  and  $j < l$ .
3. For every pair  $0 < k < i < n$ , a candidate  $Ri^{ij}$  is never nrc linked to a candidate  $Rk^{kl}$ .
4. There exists a candidate  $Rn^{ij}$  that is nrc linked to a candidate  $Rk^{kl}$  ( $k=n$  and  $k=0$  are possible).

If there exists a MBraid for  $R0^{i1}$  and the candidate  $R0^{i1}$  were true, then all candidates  $Ri^{ij}$  would be true and we would reach a contradiction, so  $R0^{i1}$  can be eliminated.

What I do with that procedure is assert  $R0^{i1}$ , then make all ECP eliminations, then some singles are discovered, we tag them all  $R1^{i1}, R1^{i2}, \dots, R1^{im1}$ , and we assert them all at once, when new singles are discovered, we tag them  $R2^{i1}, R2^{i2}, \dots, R2^{im2}$  and assert them all at once, and so on until a contradiction is reached.

If  $R0^{i1}$  can be eliminated using T&E(NS,HS), then there exists a unique MBraid that eliminates it, and we know also that there exists a braid that eliminates it, and moreover, the length of that braid is not greater than the length of any braid that eliminates it.

The candidates  $R1^{i1}, R1^{i2}, \dots, R1^{im1}, R2^{i1}, \dots, R2^{im2}, R3^{i1}, \dots, Rn^{imn}$  are the right linking candidates of a braid that eliminates  $R0^{i1}$ .

The MBraid rating of a puzzle is the minimum  $n$  such that the puzzle can be solved using MBraid of length at most  $n$ , if no  $n$  satisfies the condition, then we say that the rating is infinite (using MBraids). The MBraid rating of a puzzle is finite if and only if it is solvable using T&E(NS,HS), and the last part is true if and only if it is solvable using braids.

The following puzzle has a MBraid rating of 20 (19?)

**Code:**

```
000001002000030040005600700002800003040050060900007400007003004030020080600400300
```

and so it can be solved using braids but it can't be solved using braids of length 19 or less (BTW, it is not so hard if you use some exotic uniqueness argument 😊).

Notes:

1. I developed this before Denis published his definition of braids, only a few days ago I realized it gives a lower bound of the pB rating of a puzzle.
2. Finding minimal braids is not an easy task, and MBraids contain a lot of unnecessary information, and moreover, a Braid can be complexly embedded in a MBraid. Generally the MBraid rating is lower than the Braid rating.
3. MBraid ratings can be calculated very quickly
4. I don't think this procedure can be easily turned into a pBraids rating calculator.

[Back to top](#)

[profile](#) [pm](#)

**Red Ed**

Posted: Fri Jan 08, 2010 7:39 pm Post subject:

Joined: 06 Jun 2005  
Posts: 1007

**Mauricio wrote:**

The following puzzle has a MBraid rating of 20 (19?)

**Code:**

```
000001002000030040005600700002800003040050060900007400007003004030020080600400300
```

and so it can be solved using braids but it can't be solved using braids of length 19 or less (BTW, it is not so hard if you use some exotic uniqueness argument 😊)

What "it" is "not so hard"? I like exotic uniqueness arguments and don't want to feel I'm missing out ...!

[Back to top](#)

[profile](#) [pm](#)

**Mauricio**

Posted: Fri Jan 08, 2010 9:38 pm Post subject:

**Red Ed wrote:**

**Mauricio wrote:**

The following puzzle has a MBraid rating of 20 (19?)

**Code:**

```
000001002000030040005600700002800003040050060900007400007003004030020080600400300
```

and so it can be solved using braids but it can't be solved using braids of length 19 or less (BTW, it is not so hard if you use some exotic uniqueness argument)

What "it" is "not so hard"? I like exotic uniqueness arguments and don't want to feel I'm missing out ...!

The puzzle is automorphic (reflex along main diagonal and swap digits 1-9,2-6,3-4), then you can make some eliminations in the diagonal (explicitely, you can eliminate 1,2,3,4,6 solved using singles only).

[Back to top](#)

[profile](#) [pm](#)

Display posts from previous:

[new topic](#)

[postreply](#)

[Sudoku Players' Forums Forum Index -> Advanced solving techniques](#)

[Goto page](#)

Page 9 of 10

[Stop watching this topic](#)

Jump to: