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### Author

### Message

**StrmCkr**

Posted: Thu Jul 09, 2009 7:20 am Post subject:



Joined: 05 Sep 2006  
Posts: 478  
Location: Winterpeg

#### Quote:

deletion phase

which part of the deletion phase the +2 - 1 phase or the after affect

which has the affect of modify the logic sets the grid starts with.

of removing super flours clues.

(which merely reinforces the complexity of logic needed)

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**m\_b\_metcalf**

Posted: Thu Jul 09, 2009 7:23 am Post subject:



Joined: 15 May 2006  
Posts: 2207  
Location: Berlin

#### denis\_berthier wrote:

I imagined the following double generation process:

- 1) take the first part of a bottom-up generator and get a non complete grid G1 with a unique solution
- 2) with the second part of the generator obtain a minimal puzzle P1
- 3) let G2 be the complete (solution) grid obtained from G1
- 4) with exactly the same second part (this is very important) obtain a minimal puzzle P2

Question: is there any correlation between P1 and P2:

- number of clues
- SER
- NRCZT

**Mike**, do you think your bottom-up generator could be adapted to do this? (10,000 couples of puzzles would be enough for such computations.)

I added just three statements to my program, and got the following result in 500s:

**Code:**

```

Bottom-up
-----

Number:      11177
Average:    23.88798

    20      0
    21     94
    22    918
    23   3041
    24   4040
    25   2362
    26   631
    27    81
    28    10
    29     0

Top-down
-----

Number:      11177
Average:    24.37049

    19      0
    20      1
    21     28
    22    390
    23   1985
    24   3779
    25   3332
    26   1354
    27    279
    28     28
    29      1
    30      0

```

I'll e-mail you the file.

Regards,

Mike Metcalf



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**denis\_berthier**

Posted: Thu Jul 09, 2009 7:29 am    Post subject:



Joined: 19 Jun 2007  
Posts: 678  
Location: Paris, France

**m\_b\_metcalf wrote:**

I added just three statements to my program, and got the following result in 500s

That's really very interesting. You've definitely proven that the difference for the number of clues is not related to the specifics of the deletion phase.

Regards

[Back to top](#)**Allan Barker**

Posted: Thu Jul 09, 2009 8:19 am Post subject:



Joined: 21 Feb 2008

Posts: 288

Location: Bangkok

**denis\_berthier wrote:****m\_b\_metcalf wrote:**

I added just three statements to my program, and got the following result in 500s

That's really very interesting. You've definitely proven that the difference for the number of clues is not related to the specifics of the deletion phase.

Regards

I think this difference, which Mike pointed out seems to be  $\frac{1}{2}$  comes about purely from the direction you approach the boundary between MS and SS grids. Maybe people with more experience can help this one out.

When approaching from the top, the first candidate removed that produces a MS grid is replaced (put back in) and a local minimum is searched for. However, replacing this candidate effectively cuts the local sample space for this search in half by assuming this candidate must be in the minimum grid, which will be true 50% of the time (within a given distance in grid space). No such problem occurs coming up from the bottom because the first candidate added that produces a SS grid is assured of being in the local minimum. So, on average the top down approach will be higher (than necessary) by one candidate 50% of the time.

I have waived my hands, they are dry. 😞

[Back to top](#)**David P Bird**

Posted: Thu Jul 09, 2009 8:45 am Post subject:



Joined: 17 Sep 2008

Posts: 60

Location: Middle England

I think what lies behind **StrmCkr's** thinking is something like this:

If we have supplied sufficient clues to solve a certain key part of a puzzle with difficulty, adding random clues to allow the rest of the puzzle to be completed would usually provide a much easier route to solve the key area. To prevent that, we would need to customise the balance of the givens to specifically cover the relatively unimportant fringe areas only.

On another subject, I have a gut feeling that the number and nature of the two-digit unconditional sets have a big role to play in the potential difficulty of a puzzle.

Here is one illustrative example in a grid with a single unconditional set for a digit pair:

**Code:**

	a	a	
a		b	b
		a	a
a	a	a	
a	a		
	a	b	
			b

The cells marked 'a' are all connected by an orthogonal loop with alternate legs along rows and columns. This leaves four further 'b' cells in a rectangle which form a "NOT a UR". If no given is provided for the 'b' cells, there is a chance that they won't be solvable until one of the 4 'a' cells in a common box has been resolved, which could restrict the solution path.

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**eleven**

▢ Posted: Thu Jul 09, 2009 10:07 am    Post subject:


 Joined: 10 Feb 2008  
 Posts: 331

One more puzzling result. I generated minimal puzzles bottom up without dropping any clues, i.e. i only took unique puzzles, if they were minimal from the adding clue phase.

Maybe Mike can repeat it to exclude coding errors.

**Code:**

```

20:      3
21:      46
22:     524
23:    2301
24:    3757
25:    2549
26:     710
27:     106
10000 puzzles, av. clue number 24.0804

```

To my surprise the average clue number only is slightly higher and still clearly under the value from top down generation.

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**m\_b\_metcalf**

▢ Posted: Thu Jul 09, 2009 10:19 am    Post subject:

**eleven wrote:**

Maybe Mike can repeat it to exclude coding errors..

 Joined: 15 May 2006  
 Posts: 2207  
 Location: Berlin

After the adding-clue phase I typically have 30-40 clues. A quick run gave zero minimal puzzles.

Regards,

Mike Metcalf

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eleven

Posted: Thu Jul 09, 2009 10:30 am Post subject:

Joined: 10 Feb 2008  
Posts: 331**m\_b\_metcalf wrote:****eleven wrote:**

Maybe Mike can repeat it to exclude coding errors..

After the adding-clue phase I typically have 30-40 clues. A quick run gave zero minimal puzzles.

It took some hours to get the 10000 puzzles.

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coloin

Posted: Thu Jul 09, 2009 11:13 am Post subject:

Joined: 06 May 2005  
Posts: 1017  
Location: Oxford

I think the decreased clues in the "bottom up" method can be explained.

The number of puzzles within a  $\{-1+1\}$  or  $\{-2+2\}$  is greater in easier puzzles than in harder puzzles. Therefore when you are picking clues to complete the puzzle there will be more easy puzzles.

Why might this be...?

An easy [singles] puzzle if you remove a clue - still partially completes with singles - and the  $n-1$  subpuzzle will tend to have less "other grid solutions". Less "other grid solutions" implies that there will be more  $\{+1\}$  ways to complete the puzzle. All the puzzles generated from the  $\{n-1\}$  subpuzzle will have the singles which were in the subpuzzle. So all will tend to be easy.I have long thought about the analysis of the  $\{n-1\}$  subpuzzles in "hard" puzzles. Perhaps the lack of inferred clues in ALL the  $n-1$  subpuzzles tends to imply a hard puzzle.

C

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Allan Barker

Posted: Thu Jul 09, 2009 1:36 pm Post subject:

Joined: 21 Feb 2008  
Posts: 288  
Location: Bangkok**Allan Barker wrote:****denis\_berthier wrote:****m\_b\_metcalf wrote:**

I added just three statements to my program, and got the following result in 500s

That's really very interesting. You've definitely proven that the

difference for the number of clues is not related to the specifics of the deletion phase.  
Regards

I think this difference, which Mike pointed out seems to be  $\frac{1}{2}$  comes about purely from the direction you approach the boundary between MS and SS grids.

I have some results for the following

**A):** How to make a top down generator produce (Edit) average clue sizes of a bottom up generator.

**B):** Why the top down and bottom up generators differ by  $\frac{1}{2}$ .

These experiments are all done with a top down generator.

**Precursor = P:** All experiments include: (random 81 clue grid) + top down until removal of A produces a multi-solution grid.

**Experiment 1** P + Re-place A, minimize puzzle.

**Experiment 2** P + don't re-place A, add one random clue B to make valid puzzle, minimize puzzle.

**Experiment 3** Perform both exp 1 and exp 2 on the same puzzle, Choose smaller of the two minimal puzzles.

Experiment 1 is as per normal for a top down approach.

Experiment 2 produces a second version of the same puzzle with same number of clues that differs only by A versus B.

Experiment 3 Combining exp 1 and exp 2 is the same process with double the effective search space for a minimal puzzle

Explanation: Re-placing A in the top down approach effectively cuts the search space for a minimal puzzle in half (one clue of N) relative to a bottom up approach, (see previous post above) Doubling the search space in experiment 3 should then produce results (eg, average number of clues) similar to a bottom up generator.

Edit: As noted by Eleven below, although Exp 3 produces the same mean clue size as the bottom up, the ditribution is tighter, i.e., the there are 5% more 24's (41.6 to 36.4)

**Results:** Adding clue B instead of clue A should produce no difference from replacing A.

Combining A and B doubles the effective search area and should thus produce similar mean clue values to a bottom up generator.

#### Code:

```
C 19      0      Experiment 1
C 20      1      Re-place A, minimize puzzle
```

```

C 21      43
C 22      694
C 23      3379
C 24      6886
C 25      5983
C 26      2440
C 27      497
C 28      70
C 29      7
C 30      0
N=20000 avg = 24.3885

C 19      0      Experiment 2
C 20      1      Don't re-place A
C 21      47      Find 1 random clue B to make
valid grid. minimize puzzle
C 22      740
C 23      3472
C 24      6837
C 25      5884
C 26      2463
C 27      505
C 28      46
C 29      5
C 30      0
N=20000 avg = 24.3733

C 19      0      Combine Exp 1 + Exp 2,
C 20      0      Choose smallest minimal puzzle
C 21      72
C 22      1366
C 23      5834
C 24      8318
C 25      3821
C 26      556
C 27      33
C 28      0
C 29      0
C 30      0
N=20000 avg = 23.8125

```

Last edited by Allan Barker on Fri Jul 10, 2009 1:36 am; edited 1 time in total

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**StrmCkr**

Posted: Thu Jul 09, 2009 2:47 pm    Post subject:

[!\[\]\(2b376d1a92330ab09dad2665d2f89bf5\_img.jpg\) quote](#)

Joined: 05 Sep 2006  
Posts: 478  
Location: Winterpeg

#### Quote:

Results: Adding clue B instead of clue A should produce no difference from replacing A.  
Combining A and B doubles the effective search area and should thus produce the same results as the bottom up generator.

adding clue B can change the # of minimized clue...

doing this changes the preset logic bases and should effectively mimic a bottom up generator as minimality is no longer depend on the preset logic bases from the starting grid.

david  
thanks you for the rewrite

yes that was my point exactly in bottom up generators it has the tendency to fill in a key area randomly and prevent complex logic sets.

in top down the logic created by the starting grid aid by staying constant where by checking the solution count u can determin if you can still remove a clue or not.

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**m\_b\_metcalf**

Posted: Thu Jul 09, 2009 3:03 pm Post subject:



Joined: 15 May 2006  
Posts: 2207  
Location: Berlin

**eleven wrote:**

**m\_b\_metcalf wrote:**

**eleven wrote:**

Maybe Mike can repeat it to exclude coding errors..

After the adding-clue phase I typically have 30-40 clues. A quick run gave zero minimal puzzles.

It took some hours to get the 10000 puzzles.

Indeed. So I made a short run:

**Code:**

```
Number:      157
Average:    24.10191

 21      0
 22      7
 23     29
 24     57
 25     46
 26     15
 27      1
 28      1
 29      0
```

Looks comparable?

Mike Metcalf

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**coloin**

Posted: Thu Jul 09, 2009 3:11 pm Post subject:



Yes, in the bottom up there is an advantage in being able to pick a [unique] clue [from all the grid solutions of the subpuzzle] which gives a valid puzzle.

Joined: 06 May 2005  
Posts: 1017



Location: Oxford

They will tend to be easier puzzles if there are inferred clues [singles] already in the subpuzzle - which they tend to be if the subpuzzle is able to be completed to puzzle with one more clue..

This disadvantages the top down method where the solution grid is constant.

C

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**eleven**

Posted: Thu Jul 09, 2009 7:02 pm    Post subject:



Joined: 10 Feb 2008  
Posts: 331

**Allan Barker wrote:**

However, replacing this candidate effectively cuts the local sample space for this search in half by assuming this candidate must be in the minimum grid, which will be true 50% of the time (within a given distance in grid space).

I don't understand this. The top down generation is nothing than looking for a local minimum in a whole grid, done by eliminating clues in random order. Some of them would lead to multi solution puzzles, so they are not eliminated.

Now you say, when you arrive at the first number, which cannot be eliminated, you replace it by another one, thus building local minima in 2 grids now. And if you take the lower one, this would "produce the results of a bottom up generator".

Why only the first number, why [edit] the number you cannot drop at this stage ? And what does that have to do with bottom up generation ?

Also only the mean clue value really compares to the bottom up distribution. E.g. in your sample there are 5% more 24's (41.6 to 36.4).

Anyway, it was another surprise for me, that you could lower the mean value that much with this simple change.

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**Red Ed**

Posted: Thu Jul 09, 2009 9:11 pm    Post subject:



Joined: 06 Jun 2005  
Posts: 549

This thread seems to be getting a bit mixed up.

Are you all just trying to understand why different puzzle generators exhibit different statistics? Or trying to generate puzzles with few clues? Both perfectly reasonable aims, but surely unrelated to the original topic. (Not trying to be Thought Police here: just genuinely confused.)

Or maybe you're trying to generate minimal puzzles in an unbiased way. In which case I'll repeat what I said on the "How many minimal sudokus has an average grid" thread yesterday, that the average number of clues that you should be aiming for is in the region of 26.*something*. You're a long way off that ...

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