



## Sudoku Players' Forums

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#### Author

#### Message

**m\_b\_metcalf**

Posted: Wed Jun 24, 2009 2:11 pm Post subject:



Joined: 15 May 2006  
 Posts: 2106  
 Location: Berlin

#### denis\_berthier wrote:

Is your generator available? Or is there any place where the basic principles it uses are defined? Or can you state them in a few words?

In any case, I'm interested by your file of 110840 puzzles. It'd be a good way to check my results about the nrczt and SER ratings and to confirm that they don't depend on the generator.

I generate a grid by filling its first row with the nine digits in a random order, obtained using *random\_number* (a Fortran 95 intrinsic function), and then adding subsequent rows of randomly arranged digits, sorting their order as necessary to avoid clashes with digits already in place on previous rows or already in the current box. If this cannot be done, a fresh set of random numbers is used. For the third and sixth rows, an additional check is required that the box constraint is also fulfilled. Also, a deadlock condition can arise on row 6 when the three digits missing from an almost completed box have already been assigned to a single column above the box. If this occurs, the program restarts at row 4.

I generate a puzzle by selecting, say, 60 clues from a grid at random and then removing further clues at random, checking the puzzle remains minimal at each step.

This is part of a larger program for which you would need a Fortran 95 compiler (of which there are two free ones available but I use the highly optimizing Intel v. 10).

If you send me a PM with your e-mail address I will send you the puzzle file.

Regards,

Mike Metcalf



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**denis\_berthier**

Posted: Wed Jun 24, 2009 2:22 pm Post subject:



Joined: 19 Jun 2007  
 Posts: 601  
 Location: Paris, France

#### m\_b\_metcalf wrote:

I generate a grid by filling its first row with the nine digits in a random order, obtained using *random\_number* (a Fortran 95 intrinsic function), and then adding subsequent rows of randomly arranged digits, sorting their order as necessary to avoid clashes with digits already in place on previous rows or already in the current box. If this cannot be done, a fresh set of random numbers is used. For the third and sixth rows, an additional check is required that the box constraint is also fulfilled. Also, a deadlock condition can arise on row 6 when the three digits missing from an almost completed box have already been assigned to a single column above the box. If this occurs, the program restarts at row 4.

I generate a puzzle by selecting, say, 60 clues from a grid at random and then removing further clues at random, checking the puzzle remains minimal at each step.

I need some time to think about whether this is not biased.

**m\_b\_metcalf wrote:**

If you send me a PM with your e-mail address I will send you the puzzle file.

Thanks, this is the easiest way.

regards.

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**coloin**

Posted: Wed Jun 24, 2009 4:00 pm Post subject:



Well we investigated the generation of unbiased grids here, inc solution grids from puzzles made from suexg.

<http://www.sudoku.com/boards/viewtopic.php?t=5128&start=0>

Essentially if you have an average count of 11.58 U4s in your [solution] grids your grids are not biased. Grids made with suexg had average value 10.67

**RedEd wrote:**

Back to size-4 unavoids: the average number is exactly 320784513273 / 27704267971, or roughly 11.58 per grid.

However I still feel that the method of removing clues to minimality predisposes slightly to smaller puzzles.

Take this random solution grid.

**Code:**

```
246518739791342658583769214875294361129635847634871925352187496918426573467953182
solution grid
```

**Code:**

```
lines:206083 average clues:24.342556 - similar to random grids
20 9
21 539
22 7631
23 36975
24 71389
25 60392
26 23904
27 4723
28 490
29 30
30 1
```

because there are so many minimal puzzles in a single grid, let us look at a 40-clue subgrid...[25clue puzzle plus 15 more extra clues.]

**Code:**

```
.4.....97....2.585...6..1...5....6....63...7.....192...21.....9.8.....3.679.....
25puzzle
24..18..97..3.2.585.3.6..1...5.94.6.1..63...7..4..1925..2187...9.8..6..3.679...82
25plus15puzz
```

If we generate 1000000 puzzles from this subgrid we get 372190 different puzzles [almost certainly there are more puzzles, especially with 27-29 clues]

**Code:**

```
puzz:372190 average clues:24.897902
```

```

21  45
22  1257
23  21428
24  105884
25  148341
26  77159
27  16721
28  1330
29  25

```

compare with the clue stats from 500,000 puzz

**Code:**

```

puzz:257081 average clues:24.778035
21  45
22  1247
23  19460
24  81487
25  98436
26  46276
27  9416
28  699
29  15

```

If you generate "Only" 16000 puzzles from the 40 clue subgrid you get this distribution

**Code:**

```

puzz:15266 average clues:24.392637
21  27
22  400
23  2455
24  5584
25  4645
26  1798
27  340
28  16
29  1

```

there is a considerable skew towards smaller puzzles

C

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**denis\_berthier**

▢ Posted: Wed Jun 24, 2009 4:57 pm    Post subject:



Joined: 19 Jun 2007  
Posts: 601  
Location: Paris, France

**coloin wrote:**

Well we investigated the generation of unbiased grids here, inc solution grids from puzzles made from suexg.  
<http://www.sudoku.com/boards/viewtopic.php?t=5128&start=0>  
Essentially if you have an average count of 11.58 U4s in your [solution] grids your grids are not biased. Grids made with suexg had average value 10.67

Thanks for the reference. I need more time to study this. The U4 argument is interesting for *solution grids*. But the question I'm interested in here is puzzles, not solution grids.  
I think it would be very difficult to test the unbiasedness of every step in the generation process of a sequence of minimal puzzles. That's why I tried several direct tests, based on the autocorrelation of numerical functions of the sequence.

As for your examples, I'm not sure what you want to prove, but no stats can be done based on a single solution grid. Starting from a different one, you could obtain very different results.

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**coloin**

▢ Posted: Wed Jun 24, 2009 10:50 pm    Post subject:



Joined: 06 May 2005  
Posts: 986  
Location: Oxford

Indeed, you are dealing with minimal puzzles, and that said, the degree of bias for the solution grids made by suexg is not that great.

However I was demonstrating that smaller puzzles are produced preferentially by the "clues removal" method of these programs.

I appreciate that taking puzzles from a single grid or subgrid might seem unwise.

I would hazard a guess that , w.r.t ratings, 1M "random" puzzles from a single grid would be as representative as 1M random puzzles from 1M random grids - but I could well be wrong. The clue distribution from this complete random grid is similar to your distribution.

I would suggest that the [lack of] correalation between the number of clues and the rating isnt just as clear cut as you as indicate.

here are the ratings from the initial 64000 of your 1M series, which you may chose to confirm.

**Code:**

```
173      28-puzzles Mean SER 5.12 Mean NRCZT-level 2.66
21972    24-puzzles Mean SER 3.68 Mean NRCZT-level 1.89

Total 1M puzzles Mean SER 3.78 Mean NRCZT-level 1.94
```

This doesnt look like a chance occurance - perhaps confirming that large puzzles tend have a higher than average rating, but I'm not sure why.

C

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**denis\_berthier**

Posted: Thu Jun 25, 2009 5:02 am Post subject:



**Coloin,**

Joined: 19 Jun 2007  
Posts: 601  
Location: Paris, France

Here are the mean number of clues and standard deviation for each nrczt-level in the sudogen0\_1M collection:

**Code:**

Level	#Puzzles	E(Clues)	s(Clues)
1_0	417624	24.29	1.089
1	120618	24.22	1.11
2	138371	24.35	1.12
3	168355	24.52	1.13
4	123153	24.60	1.14
5	24187	24.63	1.14
6	5511	24.68	1.13
7	1514	24.69	1.13
8	473	24.67	1.10
9	130	24.45	1.02
all	1M	24.38	1.11

Obviously, nothing can be concluded from this, the maximum deviation (0.31) of each subset from the global mean (24.38) being much smaller than the global standard deviation (1.11).

Conversely, here is, for each number of clues (except 20, 29 and 30, which don't have enough instances to be meaningful), the means and standard deviations for the nrczt-level and the SER:

**Code:**

#Clues	#Puzzles	E(Level)	s(Level)	E(SER)	s(SER)
21	2428	1.58	1.04	3.03	2.0
22	34548	1.69	1.13	3.27	2.16
23	172512	1.78	1.20	3.44	2.28

24	342335	1.88	1.26	3.65	2.38
25	297838	2.01	1.31	3.90	2.46
26	122116	2.17	1.36	4.22	2.53
27	25315	2.38	1.40	4.63	2.56
28	2686	2.64	1.44	5.11	2.56
all	1M	1.94	1.29	3.77	2.42

Now, the question is, what conclusions can be drawn from this?

Firstly, it seems that there is indeed a tendency for a slightly higher mean complexity with increasing number of clues (whether we consider nrczt or SER).

But one should consider that the maximum deviation (0.7 for NRCZT, 1.44 for SER) of the mean of each subset from the global mean (NRCZT = 1.94 or SER = 2.42) is much smaller than the global standard deviation (1.29 for NRCZT, 2.42 for SER).

So, it seems that there is a trend, but it can't be used for predictions, due to the very low correlation coefficients (0.12) and the very large standard deviations.

Secondly, there is a different question: does this slight trend indicate any bias in the suexg generator?

There's no reason to suppose so. The slight trend (if confirmed) may be real, i.e. it may exist in the set of all the minimal puzzles.

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**denis\_berthier**

Posted: Thu Jun 25, 2009 5:37 am Post subject:

[quote](#) [edit](#)

Joined: 19 Jun 2007  
Posts: 601  
Location: Paris, France

### Top sudogen0\_1M

Here is now a short list of "interesting puzzles" from the sudogen0\_1M collection.

They have been chosen because they satisfied at least one of the following "(relatively) extreme" conditions:

- SER > 9.1,
- NRCZT >= 9.

#### Code:

```
#puzzle      Puzzle
              SER      NRCZT  #clues
707
4..3..6.8..5..1.3..16.4...7.7.....8.....2....51..637...2.9.8.....1.....4..9
9.2      12      25
2035
...7...637...4.9..6.95....8.....7...5.6.....9...2..16..3..8..224.....7.....9..
9.2      10      24
88857
3.....41.....69578.3..51.64.78.4....3.5...7.....9....6..2...9..1...5.....6.
9.2      12      26
117617
91.....7..2...8....3..16..7..6.2..5.1.....6....91.....5.....4.8.6.2.8.7..3
9.2      12      24
124235
1.....6..6..43...9....1..7..8..4.25.1...76.....5.....8.2..4.9..5.8..3..7..
9.3      12      24
143634
..5.3.4.2....54.9.1.....19.4..8.4.3..72....85....99..6.8.....7.27..5...
9.2      10      26
175675
..85....4.....2..3..6.9.8....82...2....3...7.9.1...9.8..6....52...7....7....1
9.2      11      23
188892
...5...476...4..3..9....1....2...5..7.....8...6...1.9..46.....6..1..28..9.24..
9.2      13      24
200753
...6.3..4..2...1..1.4..8...86..9.3....7.....4...816.7.....8..9....7...34...2..
9.2      10      24
298676
2...5...9..6...5.....7.1.4.5.....6.8.3.6.4....8..7....1...43..2...89..9...1..5.
9.2      13      25
346155
7...63...4...76...3.....9...45.23.4...7.47..8...1..72.....1..492.....3.51.
9.2      10      27
```

```

420249
...37.4....4..5.2.5.....872..9.....6..24...78.....4...17.5.1.....5.....8.9
 9.2      11      24
425702
..8..2....278...3.9....1....6.....3..95..5..1.4.61...592.4....8...5...1..7..
 9.2      12      25
431065
.3.....7.9....16...67....1..9.467...61.5.4....3...1.....8.....1...4..495716.
 9.2      12      27
618406
15.8....2...4.19.....1..3.4....78...6..2.1.....8..9....2.9..3....4.5...71....6
 9.3      12      25
631828
1.57....4..6..53.....8...5...7.5...94.....6.2.6.9.....7.....6...3.92.3....41.
 9.2      10      25
641898
..74.2...48....9..1..5.....6.19.34.4.....7..8.9...2.5...3.....1.6.94.3..7.
 9.2      10      26
717866
...51....5.4.....21....9..7..6.42...3..8....9.7...83....2.1.7..8....9.....7.5.
 9.2      11      24
739105
..7..6.8....2...46....3.2..41.....27.....5...2.19..4..16.5...38.12...95.....
 9.2      9       26
792244
1.....43..5.....938...1..92.5..9..6.8.23.....9....4..6.75...7.....6...1..9.
 9.2      11      25
810153
..64.....7..5....9....6..8.....5.8..2.9..3....83..7..5.4.37.1.....7...12.56.
 9.2      9       25
845088
.8..1...6..3...5..2....7.....2.3.....8.947.8...2.6.....9.73..2.4.....5....
 9.2      12      22
942062
.4.....96....98..7.....2..7.13....8.....2.1...5.9.....2.5..5..4...78..1.7...4
 9.2      12      24

```

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**m\_b\_metcalf**
☐ Posted: Thu Jun 25, 2009 6:42 am    Post subject:



Joined: 15 May 2006  
 Posts: 2106  
 Location: Berlin

For what it's worth, I generated an hour's worth of puzzles all from the [same grid](#). The summary is:

**Code:**

```

Number:      54074
Average:     24.25319

    20      4
    21     194
    22    2443
    23   10709
    24   19050
    25   14842
    26   5588
    27   1117
    28    120
    29      7

```

Another game I played was to run a tiny sample of yesterday's puzzles through a program that pair-wise changes the values of the clues (but not their positions) and removes any clue that thereby becomes redundant. This I repeated several times. The result:

**Code:**

```

Iteration 1

    Number:      143
    Average:     20.45

    17      0
    18      3
    19     14
    20     64
    21     42

```

```

      22      17
      23      3
      24      0

Iteration 2

Number:      143
Average:     20.09

      17      0
      18      3
      19     30
      20     71
      21     31
      22      6
      23      2
      24      0

Iteration 3

No change.

```

Regards,

Mike Metcalf

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**denis\_berthier**

▢ Posted: Thu Jun 25, 2009 12:23 pm    Post subject:

[quote](#) [edit](#)

Joined: 19 Jun 2007  
Posts: 601  
Location: Paris, France

**m\_b\_metcalf wrote:**

I generate a grid by filling its first row with the nine digits in a random order, obtained using *random\_number* (a Fortran 95 intrinsic function), and then adding subsequent rows of randomly arranged digits, sorting their order as necessary to avoid clashes with digits already in place on previous rows or already in the current box. If this cannot be done, a fresh set of random numbers is used. For the third and sixth rows, an additional check is required that the box constraint is also fulfilled. Also, a deadlock condition can arise on row 6 when the three digits missing from an almost completed box have already been assigned to a single column above the box. If this occurs, the program restarts at row 4.

It seems that not all the rows are dealt with in the same way and this may introduce a bias, although which kind of bias it can be is not clear for me.

**m\_b\_metcalf wrote:**

I generate a puzzle by selecting, say, 60 clues from a grid at random and then removing further clues at random, checking the puzzle remains minimal at each step.

Am I wrong to say it is the same method as *suexg*?

It is very difficult to analyse how much the (possible) bias in the first step is smoothened by the second step.

Anyway, the results I obtain are significantly different on several points from those I obtained with *suexg* (see next post).

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**denis\_berthier**

▢ Posted: Thu Jun 25, 2009 12:25 pm    Post subject:

[quote](#) [edit](#)

Joined: 19 Jun 2007  
Posts: 601  
Location: Paris, France

For a set of 50,000 random puzzles provided by *m\_b\_metcalf* with his generator, here is, for each number of clues, the means and standard deviations for the *nrczt*-level and the *SER* (these last variables don't have enough instances to be meaningful for #clues = 20, 29 and 30):  
(I used only the 50,000 first puzzles in a series of 110,000).

**Code:**

```

#Clues #Puzzles  E(Level)  s(Level)  E(SER)  s(SER)
20      2      0.95      0.05      1.6     0.10

```

21	136	1.33	0.80	2.64	1.63
22	1801	1.34	0.84	2.57	1.58
23	8736	1.31	0.82	2.49	1.55
24	17145	1.26	0.78	2.41	1.50
25	14852	1.22	0.73	2.32	1.38
26	5952	1.19	0.69	2.26	1.31
27	1225	1.14	0.58	2.15	1.11
28	147	1.10	0.45	2.02	0.71
29	4	0.9	0.0	1.95	0.29
30	0				
all	50k	1.25	0.76	2.41	1.48

$E(\text{clues}) = 24.36$

$s(\text{clues}) = 1.12$

$E(\text{NRCZT}) = 1.25$

$s(\text{NRCZT}) = 0.76$

$E(\text{SER}) = 1.95$

$s(\text{SER}) = 1.48$

It can be noted that:

- contrary to the sudogen0\_1M case, the mean level (NRCZT and SER) is (slightly) decreasing with the number of clues. But, here again, the maximum deviation of the mean value is much less than the global standard deviation. So, again, this may not be very meaningful;
- the mean number of clues is very close : 24.36 instead of 24.38 (and the standard deviations also (1.12 instead of 1.11));
- the mean NRCZT is much smaller : 1.25 instead of 1.94
- the mean SER is much smaller : 1.95 instead of 3.77

The classification according to NRCZT levels shows that:

- the max SER is 9.0
- the max NRCZT is 10 (but with only one instance; there's no puzzle with NRCZT = 9 and only one instance with NRCZT = 8)

#### Code:

```

Level Number
1_0 32146
1 8055
2 5768
3 2464
4 1327
5 201
6 27
7 10
8 1
9 0
10 1
11 0
12 0
13 0

```

This shows that:

- there are many more puzzles at level 1\_0 (i.e. solved by singles) than with suexg: 64.3% instead of 41.7%
- there are fewer puzzles at levels > 7 : 4/100.000 instead of 66.7/100.000.

Globally, m\_b\_metcalf's generator produces easier puzzles than suexg (wrt to the NRCZT or SER ratings). This may be related to a bias introduced by the first generation phase, but the nature of this (possible) bias is not clear for me.

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**m\_b\_metcalf**

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▢ Posted: Fri Jun 26, 2009 1:56 pm Post subject:

[quote](#)



**denis\_berthier wrote:**

Joined: 15 May 2006  
 Posts: 2106  
 Location: Berlin

Average # of clues: 24.36532 vs 24,38

**Code:**

```
#Clues    #Puzzles    #Puzzles*1,000,000/51492 vs my results
20         2          39 vs 44
21        142         2,470 vs 2,428 (should be 2758!)
22       1853        35,986 vs 34,548
23       8996       174,797 vs 172,512
24      17656      342,888 vs 342,335
25     15306     297,250 vs 297,838
26      6127     118,989 vs 122,116
27      1257     24,412 vs 25,315
28       149      2,894 vs 2,686
29         4        78 vs 168
30         0         0 vs 10
```

Denis,

Thanks for looking into this. As far as a bias/discrepancy is concerned, I have spent some time scratching my head. The grid generator was tested by **RedEd** some years ago and found satisfactory (I can no longer find the post). I think that a minor difference, possibly sufficient to cause the discrepancy, is in the way cells are removed. In an attempt to make my program more efficient, I make two passes over the clues, in the first removing those shown to be redundant using simple logic, and in the second removing those shown to be redundant using backtracking. In order to make a comparison, I have now generated a second file where removal is performed in a single pass. The summary for the same number of puzzles is:

**Code:**

```
Number:      51492
Average:    24.40608

20         3    ->        58
21        139        2699
22       1663       32291
23       8867      172201
24      17309      336149
25     15409     299250
26      6395     124194
27      1508     29032
28       187      3632
29        11       214
30         1        19
```

showing a small but clear difference. If you wish, I can send you this second file for you to analyse further.

Have we learnt something?

Regards,

Mike Metcalf

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**denis\_berthier**

Posted: Fri Jun 26, 2009 4:50 pm    Post subject:

 [quote](#)  [edit](#)

**m\_b\_metcalf wrote:**

As far as a bias/discrepancy is concerned, I have spent some time scratching my head. The grid generator was tested by **RedEd** some years ago and found satisfactory (I can no longer find the post).

The only kind of test of unbiasedness for complete grids I heard of is the one referred to by Coloin in a previous post, related to U4s (<http://www.sudoku.com/boards/viewtopic.php?t=5128&start=0>).

But a statistical test is only a test. If negative, then there is a bias wrt to this test, but there may be no bias wrt to another test; if positive, then there's no bias wrt to this test, but there may be a bias wrt to another test.

Joined: 19 Jun 2007  
 Posts: 601  
 Location: Paris, France

It is like the Tower of Pisa. Depending on which side you're looking, either it leans or it doesn't. Except that it is much more complex: in our case, there can be hundreds of different angles of view. Moreover, it is very unclear how passing or not the U4 test on complete grids can have any impact on a possible bias of minimal puzzles generated from them.

**m\_b\_metcalf wrote:**

I think that a minor difference, possibly sufficient to cause the discrepancy, is in the way cells are removed. In an attempt to make my program more efficient, I make two passes over the clues, in the first removing those shown to be redundant using simple logic, and in the second removing those shown to be redundant using backtracking. In order to make a comparison, I have now generated a second file where removal is performed in a single pass.

I guess there were lots of cases for which the first pass was enough (Could you check this ?). That'd explain why, in your first file, there were so many puzzles that could be solved with singles. Perhaps, it could explain also that there were so few hard puzzles (first phase "almost enough" most of the time?). I think it is essential that the removal steps be completely random.

**m\_b\_metcalf wrote:**

If you wish, I can send you this second file for you to analyse further.

Yes, I'd like to do that. You can use the same mail.

**m\_b\_metcalf wrote:**

Have we learnt something?

Not very clear yet. But if the results with the new file are different, then we'll have learnt something.

Regards

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**coloin**

▢ Posted: Fri Jun 26, 2009 8:13 pm Post subject:

 [quote](#)

Very intriguing.....and I pretty much agree with all you comments.

I was surprized as any with the stats on **m\_b\_m**'s puzzle generator.

As far as the solution grid is concerned - I feel that is not much important. The distribution of puzzles from a single grid behave similarly.

Perhaps this could be confirmed. I am continuing to generate *all* the puzzles from the 40-clue subgrid. By random generation of 2M puzzles I have over 500000 puzzles .....but there probably are many more.

**Code:**

```
c:\Suxx>clusta file1.txt
lines:517883 average clues:25.028385
 21 45 [k]
 22 1258 [?k]
 23 22473
 24 127112
 25 211041
 26 123824
 27 29565
 28 2502
 29 63 [k=constant, all puzzles prob found]
```

targetting some of the larger puzzles.....

**Code:**

```
c:\Suxx>clusta file2.txt
lines:52969 average clues:26.128849
 24 1144
 25 10662
 26 24009
 27 14641
 28 2405
 29 108
```

Joined: 06 May 2005  
Posts: 986  
Location: Oxford

Most of the small puzzles have been found, but the larger ones are more difficult. An example of this is that a 30-clue puzzle was not generated randomly. ....but one has come out using gsfs program - which generates to completeness [sudoku -m -qFN -f%v file.txt] and this is still running, currently the stats are.

**Code:**

```
c:\Suxx>clusta file3.txt
lines:430886 average clues:25.167914
 21  10
 22  680
 23  14118
 24  89594
 25  173371
 26  117494
 27  32196
 28  3317
 29  105
 30  1
```

If this 40 clue subgrid is behaving itself....this may well be better reflection of the average puzzle size. But of course this is an assumption.

**gsf** also has a puzzle generator which could be analysed. Im not sure of the function which tries to generate randomly.....

C

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**denis\_berthier**

▢ Posted: Sat Jun 27, 2009 5:50 am Post subject:

 [quote](#)  [edit](#)

Joined: 19 Jun 2007  
Posts: 601  
Location: Paris, France

Thinking again of all this: it should be easy to check if the U4-test is meaningful wrt to the complexity of puzzles (measured as their NRCZT or SER levels). We just have to compute the correlation coefficient between U4 and NRCZT (or SER). 10,000 puzzles should be enough.

The only thing I'm missing for this is a (preferably fast) program that computes the U4 number of a (list of) complete grid(s). Do you know if any such program is available?

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**m\_b\_metcalf**

▢ Posted: Sat Jun 27, 2009 10:21 am Post subject:

 [quote](#)

**denis\_berthier wrote:**

I think it is essential that the removal steps be completely random.

This is clealy true, but begs the question as to what happens for an obviously biased sample. To this end, I have produced a third file in which the clue removal is again carried out in one pass, but systematically starting in r1c1 and working through to r9c9. This depletes preferentially row 1, column 1 and box 1. A 'typical' puzzle looks like this:

**Code:**

```
. . . . . . . . .
. . . . . . . 4
. . . . . 8 . 7 5
. . 1 . 7 . . .
. 2 . . . 1 . 4 .
. . 4 . . 5 2 9 .
. 3 . . . 4 . 1 .
. 4 . . 8 . . 6 7
. 9 5 . 1 7 . 2 8 SE=7.2
```

The result summary, for the same number, 51492, of puzzles is:

**Code:**

```
Number: 51492
```

Average: 25.00264

20	0
21	37
22	682
23	4318
24	12466
25	17015
26	11648
27	4309
28	905
29	109
30	3

where we see immediately the large increase in the average number of clues.

**denis\_berthier wrote:**

**m\_b\_metcalf wrote:**

If you wish, I can send you this second file for you to analyse further.

Yes, I'd like to do that. You can use the same mail.

Done.

Regards,

Mike Metcalf

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