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### THE REAL DISTRIBUTION OF MINIMAL PUZZLES

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#### Author

#### Message

**eleven**

Posted: Tue Oct 06, 2009 8:35 am Post subject:



Joined: 10 Feb 2008  
Posts: 521

#### Red Ed wrote:

I suppose the bottleneck for small samples is now the decompression step. So I guess the overall speedup coming from this new parameter is a factor of at most 3 on top of what's already been done.

When both programs are run in 32-bit mode, the decompression only needs 7-8 % of the cpu time.

But e.g. with  $p=1/10$  not only this raises above 30%, but also the input from the pipe becomes very expensive (with file input you also could use `fseek` to jump over the grids you dont take).

So i guess, that you would need about the double time then ( $1/5$  of the time to get  $1/10$  of the puzzles).

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**gsf**

Posted: Tue Oct 06, 2009 8:38 am Post subject:



Joined: 21 Sep 2005  
Posts: 3896  
Location: NJ USA

#### denis\_berthier wrote:

The procedure discussed below is `gsf|suexg-cb-optim48-U4`, i.e. generator: `gsf` (decompression of the \*.sudz files), in 32-bit mode (**gsf**: would a 64-bit mode be faster?)

I did a test on linux.i386-64 comparing a 64 bit and 32 bit executable on 006.sudz

looks like a 64 bit executable will run 33% faster

but at the moment I don't have access to a 64 bit intel mac

later today I'll put together a src package with a standalone decompressor **sudz**

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**denis\_berthier**

Posted: Tue Oct 06, 2009 8:45 am Post subject:



I've had no time for Sudoku today.

Joined: 19 Jun 2007  
Posts: 901  
Location: Paris, France

Coming home, I find nothing really new with the puzzles produced since my last post.

I deliberately didn't give the "unbiased" distribution because, with only part of the .sudz explored, there's no guarantee of having no systematic bias.

**Red Ed wrote:**

More 27s than 26s, somewhat contrary to my results; and more in total by quite a long way compared to my estimates. This just adds weight to what Denis and I both said: you can't just sample the first few \*.sudz files -- you have to do them all.

True (last sentence) but the 500,000 controlled-bias minimal produced with the original suexg-cb allowed to conclude that there are a little (1.7%) more 27s than 26s in the real distribution. This was true in all the initial sub-samples I tried from 10,000 to 500,000. So this was a very stable result.

**Red Ed wrote:**

Someone should consider adding a sampling probability parameter,  $p$ , to *suexg-cb-with-added-oompf* so that each solution grid is used (otherwise: ignored) with probability  $p$ . Then you could do a very-very-nearly-unbiased swoosh across the whole set of \*.sudz files in less time, which would be handy for posts like the previous one that look to get a quick view of the statistics.

One can always do this, but is it really worth?

After spending 2 weeks generating the .sudz files, can't we wait 2 more days for the first results with the whole collection?

The results obtained thus far are stable over time and therefore don't show any obvious dependency on the band.

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**Red Ed**

Posted: Tue Oct 06, 2009 9:26 am Post subject:



**denis\_berthier wrote:**

**Red Ed wrote:**

More 27s than 26s, somewhat contrary to my results ...

... but the 500,000 controlled-bias minimal produced with the original suexg-cb allowed to conclude that there are a little (1.7%) more 27s than 26s in the real distribution.

Gosh, yes, the suexg-cb results do say that. That's very strange. I don't understand why my experiments using suexg as the solution grids source gave counts the other way round. Will have to look into that.

**Quote:**

**Red Ed wrote:**

Someone should consider adding a sampling probability parameter,  $p$ , to *suexg-cb-with-added-oompf* so that each solution grid is used (otherwise: ignored) with probability  $p$ . Then you could do a very-very-nearly-unbiased swoosh across

Joined: 06 Jun 2005  
Posts: 763

the whole set of \*.sudz files in less time, which would be handy for posts like the previous one that look to get a quick view of the statistics.

One can always do this, but is it really worth?

After spending 2 weeks generating the .sudz files, can't we wait 2 more days for the first results with the whole collection?

It's worth it if you want to be able to do other sorts of tests (other than number of clues, and complexity) relatively quickly. Perhaps you don't want that flexibility, but others might. For another five minutes of coding, what's the issue?

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**eleven**

Posted: Tue Oct 06, 2009 11:20 am Post subject:

[quote](#)

**denis\_berthier wrote:**

I've had no time for Sudoku today.

Oh yes, you are French. Whats her name ? 😊

Joined: 10 Feb 2008

Posts: 521

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**denis\_berthier**

Posted: Tue Oct 06, 2009 9:57 pm Post subject:

[quote](#)

**eleven wrote:**

**denis\_berthier wrote:**

I've had no time for Sudoku today.

Oh yes, you are French. Whats her name ? 😊

Joined: 19 Jun 2007

Posts: 901

Location: Paris, France

... teaching 😊

Today again.

Nothing new this morning: ~ same distribution of clues.

But mean number of grids per minimal is now higher.

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**denis\_berthier**

Posted: Tue Oct 06, 2009 9:59 pm Post subject:

[quote](#)

**gsf wrote:**

later today I'll put together a src package with a standalone decompressor **sudz**

That would be very useful. Thanks.

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**denis\_berthier**

Posted: Tue Oct 06, 2009 10:34 pm Post subject:

[quote](#)

Joined: 19 Jun 2007

Posts: 901

**FINAL RESULTS FOR THE CONTROLLED-BIAS SUEXG-CB GENERATOR**

Location: Paris, France I realise that the last results I've published for suexg-cb (before we started optimising it and changing the source of complete grids) are at the bottom of this page: <http://www.sudoku.com/boards/viewtopic.php?t=14615&postdays=0&postorder=asc&start=315> and bear on only 250,000 puzzles.

I was busy with the improvements discussed above but I now have 500,000 minimals generated before them: 180,000 with the original suexg-cb version and the rest with optim46 (the first 180,000 weren't useless, as they justify using optim46, i.e. deleting the first 46 clues without doing any test).

Here are the results for the number-of-clues distribution. These are the final results as we now have a faster generator and I won't continue to generate more puzzles with this version of suexg-cb. But faster doesn't mean better or worse and the new generators don't invalidate the following results.

#### Code:

```
#clues  raw-dist  unbiased-dist * 1,000,000
19      0         0.0 (*)
20      2         0.0158 (*)
21      4         0.0920 (*)
22     615        38.589
23    9848       1585
24   60576      23563
25  154024     136602
26  168070     321050
27  83911      326513
28  20234      151844
29  2566       35193
30   147       3495
31    3        117 (*)
32    0         0 (*)

* values based on few data are not reliable.

raw mean= 25.65
raw standard-deviation= 1.120

unbiased mean= 26.56
unbiased standard-deviation= 1.113
```

The estimated mean SER and NRCZT are unchanged

SER:

raw-average = 4.147 unbiased-average = 4.48

raw-standard-deviation = 2.49 unbiased-standard-deviation = 2.53

NRCZT:

raw-average = 2.135 unbiased-average = 2.308

raw-standard-deviation = 1.340 unbiased-standard-deviation = 1.379

As usual, more detailed results, with html tables, will appear on my web pages,

as soon as I find some time for it.

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**Red Ed**

▢ Posted: Wed Oct 07, 2009 2:24 pm Post subject:



Joined: 06 Jun 2005  
Posts: 763

An idea for faster estimation of the number of 31-clue minimals ...

Pick a smaller (say 24-clue) subgrid of a solution grid. We're going to loop over all 31-clue supersets of that and will record all minimal proper puzzles that pop out. The problem is to find a way of doing this quickly.

First, do some preprocessing to check that the subgrid is minimal (i.e. no clue is implied by the others) and to find all +1 and +2 supersets that are also minimal. The latter check gives lists of single clues and pairs of additional clues that are "safe". Now loop over sets of 7 (say, if the subgrid size was 24) clues such that each clue and each clue pair within the set of 7 is safe; and, for each safe set, check first that there's a unique solution; then check that the solution is minimal.

This should be faster than the current method for 31s because you can prune the search space with those "safe" clues *and* certain classes of solver (e.g. template-based) can do a lot of preprocessing in recognition of the constant base of 24 (say) clues, so each subsequent unique-solution test can be that much quicker.

At least that's the theory. I'll try coding it over the next few days. Any comments before I start?

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**denis\_berthier**

▢ Posted: Wed Oct 07, 2009 9:01 pm Post subject:



Joined: 19 Jun 2007  
Posts: 901  
Location: Paris, France

**Red Ed,**

Do you consider multi-sol 24-clue subgrids?

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**denis\_berthier**

▢ Posted: Wed Oct 07, 2009 9:18 pm Post subject:



Joined: 19 Jun 2007  
Posts: 901  
Location: Paris, France

### **ESTIMATES for the NUMBER of N-CLUE MINIMAL PUZZLES**

I'm not really interested in the absolute number of minimals, but rather in their proportions.

Nevertheless , the above suexg-cb results give the following estimates:

#### **Code:**

```
#clues    #minimals
22        1.35529578042937e+33
23        5.5671277334354e+34
24        8.27561904095325e+35
25        4.79759013393657e+36
26        1.12755990408589e+37
27        1.14674603199864e+37
```

```

28      5.33292926612237e+36
29      1.23600037208473e+36
30      1.22733006549957e+35
31      4.1207263555285e+33 (*)
* values based on a small sub-sample are not reliable

```

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**Red Ed**
 Posted: Wed Oct 07, 2009 10:31 pm Post subject:
[quote](#)

Re multi-solution 24-clue subgrids -- yes, *only* multi-solution ones.

Joined: 06 Jun 2005  
Posts: 763

Re estimates -- thanks -- for direct visual comparison with what's gone before, could you edit (or in future post) the per-grid estimates instead, i.e. divided by  $\sim 6.67e21$ . It just saves the reader a minute or so with a calculator. Also, can you give the standard deviation of each estimate. Ta.

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**David P Bird**
 Posted: Thu Oct 08, 2009 12:39 am Post subject:
[quote](#)

Withdrawn - way off beam

Joined: 16 Sep 2008  
Posts: 165  
Location: Middle  
England

Last edited by David P Bird on Thu Oct 08, 2009 4:12 am; edited 1 time in total

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**JPF**
 Posted: Thu Oct 08, 2009 1:17 am Post subject:
[quote](#)

Joined: 06 Dec 2005  
Posts: 2921  
Location: Paris, France

**denis\_berthier wrote:**

```

#clues #minimals
22 1.35529578042937e+33
23 5.5671277334354e+34
24 8.27561904095325e+35
25 4.79759013393657e+36
26 1.12755990408589e+37
27 1.14674603199864e+37
28 5.33292926612237e+36
29 1.23600037208473e+36
30 1.22733006549957e+35
31 4.1207263555285e+33 (*)
* values based on a small sub-sample are not reliable

```

Whoa, 15 significant digits ...  
What does it mean ?

JPF

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**eleven**
 Posted: Thu Oct 08, 2009 2:42 am Post subject:
[quote](#)**Red Ed wrote:**

Joined: 10 Feb 2008  
Posts: 521

First, do some preprocessing to check that the subgrid is minimal (i.e. no clue is implied by the others) ...

I would not know how to do this quickly. suexk needed 53 sec to calculate the numbers of solutions for 240 multiresolution 24's on my PC, so one test would need about 5 secs.

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